

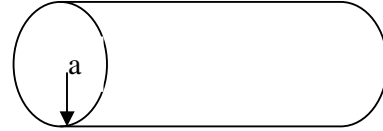


[1]. A circular wire of radius a carries a non-uniform current distribution. The current density is given as

$$J(r) = \left(\frac{J_0}{r} \right)$$

where r is the variable distance from the center of the wire and J_0 is a constant. Find:

- (a) the total current in the wire.
- (b) the magnetic field *inside* the wire as a function of r .



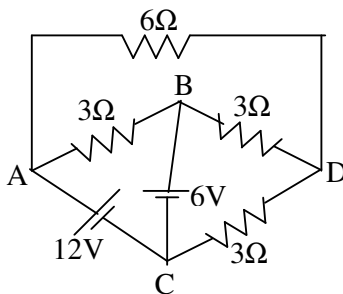
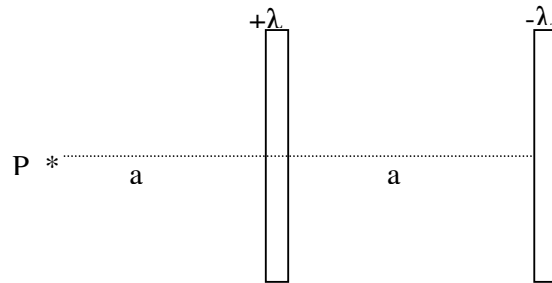
[2]. A copper wire ($\rho = 8.93 \times 10^3 \text{ kg/m}^3$; $M = 64 \text{ gr/mol}$) 50 cm long and 0.4 mm in diameter has a resistance 75Ω . If a potential difference of 40 volts is applied between the ends of the wire. (Note that there is one free electron per atom in the copper element) Determine;

- (a) the current
- (b) the current density,
- (c) the resistivity and
- (d) the electron drift speed in the copper wire.

[3]. Determine the electric field at point P perpendicular bisector plane of the two long-straight wires of the length $L=2l$ with a uniform line charge density $|\lambda|$.

Assume that $l \gg a$.

Hint:
$$\int_{-l}^l \frac{dx}{(a^2 + x^2)^{3/2}} = \frac{2l}{a^2(a^2 + l^2)^{1/2}}$$



[4]. In the given electrical circuit, what are the potential differences between the points;

- (a) AD,
- (b) BD and
- (c) AC ?

[5]. A conducting wire, whose resistance R , has a semi-circular shape of radius r as shown in Figure. If the potential difference between a and b is V ;

- (a) Express the magnetic field, B , at the center of the wire as a function of V and R
- (b) Plot the magnetic field B as a function of V .



Useful Constants: $k=9 \times 10^9 \text{ Nm}^2/\text{C}^2$ $e=1.602 \times 10^{-19} \text{ C}$ $m_e=9.11 \times 10^{-31} \text{ kg}$ $\mu_0=4\pi \times 10^{-7} \text{ N/A}$